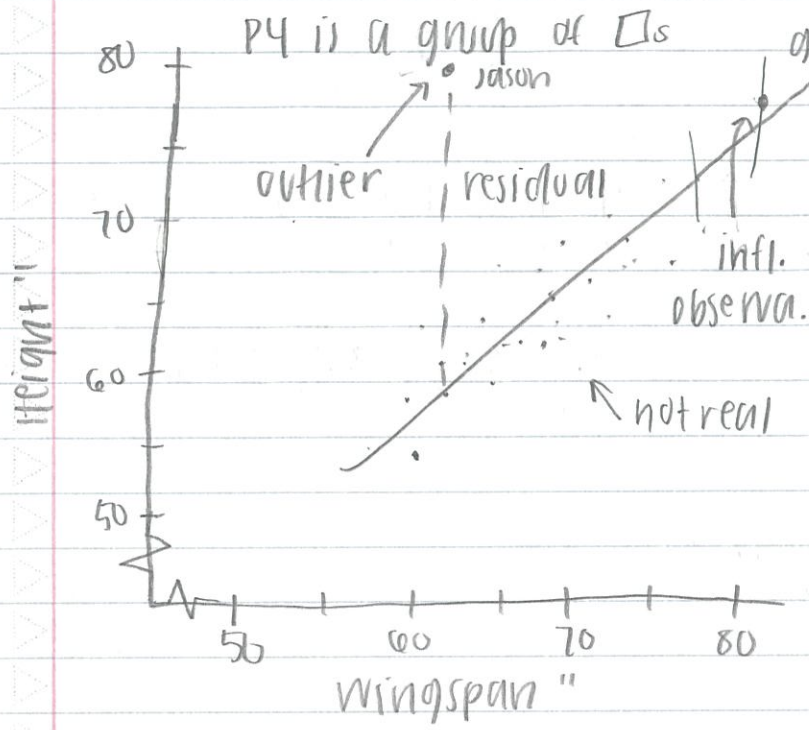
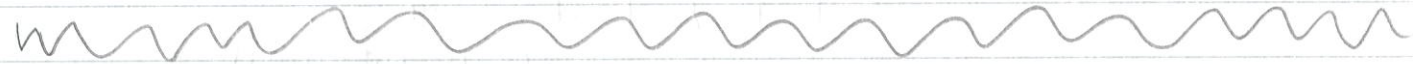


# WINGSPAN SCATTERPLOT 10/23/23

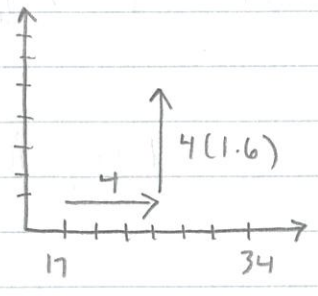


ANA:  
 + linear association  
 tr: wingspan and height are proportional (sp have sq)  
INS: (81, 80)  
OUTS: (60, 80)



## 9.2 pg 555 (ARIBOV PROBLEM 10/27)

$$b = \frac{1.6}{1}$$



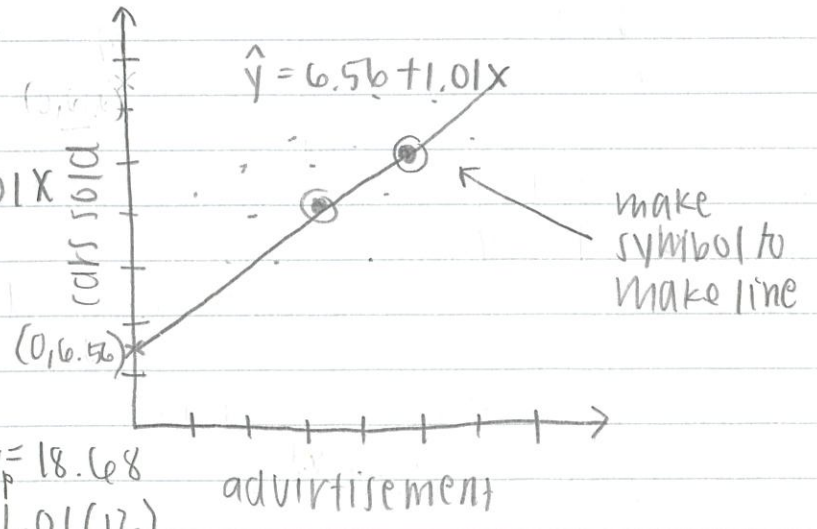
## 559 (ARS) PROBLEM

"FAMOUS" (ars)

$$\hat{y} = 6.56 + 1.01x$$

$$b = \frac{1.01}{1}$$

$$a = 6.56$$



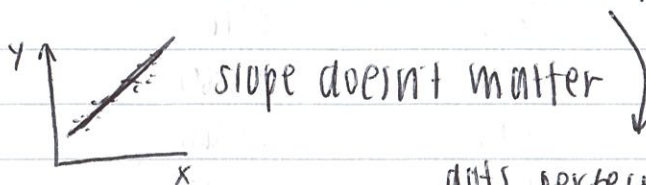
if  $X=12$ ,  $y_p = 18.68$   
 $y_p = 6.56 + 1.01(12)$



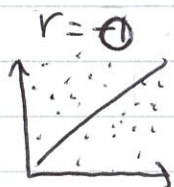
# CORRELATION COEFFICIENT 10/31

KARI PEARSON (\*not quizzed)

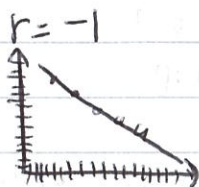
$-1 \leq r \leq 1$   $r = +1$  "perfect linear correlation"



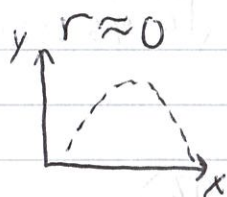
dots perfectly on line



not tight hug



"perfect linear correlation" but negative slope



not linear

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}}$$

pg 540 EXAMPLES

SAND DUMP -

$r = 0.949$  "high/strong positive correlation"

+association

as the wind speed increases, the drift rate increases (trend)

BOSTON -

-association

trend: as police officers increase, muggings decrease

$r = -0.969$  "super strong negative linear correlation"

$r^2 =$  coefficient of determination = 0.9390

park closure/warning  
baseball/ppi smw else

6.1% unexplained

(conjectures)~  
weather/time

$r^2 = 93.9\%$  of  $\text{var}(y)$  in the y (# of muggings) is explained by by least square regression line and the variation in x (# of police)

9.1 #15 HW PROBLEM CYCLONES \* draw scatterplots

strong negative linear correlation  
trend: a) the lower pressure increases, the maximum wind speed decreases

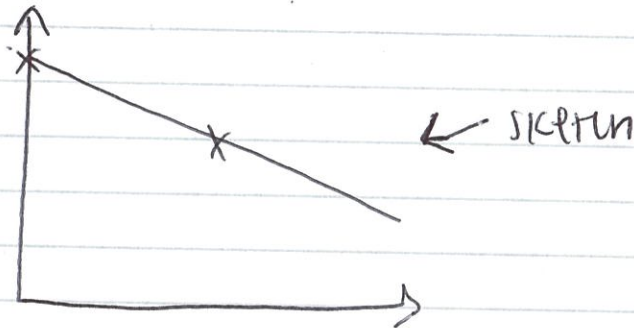
$$\bar{x} = 970.5$$
$$\bar{y} = 96.67$$

CALC 8

$$a = 1496.78$$
$$b = -1.4427$$

$$y = a + bx$$
$$y = 1496.78 + (-1.4427)x$$

x	y
970.5	96.67
0	1496



$$r^2 = 0.9796$$
$$r = -0.9897$$

y = vars stats EQ } sim like that 2nd trace value

spurious correlation - seemingly related but not (lemons and fatalities)

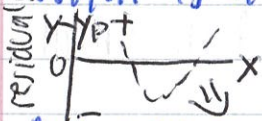
NO causation

# STUDY GUIDE 11/8

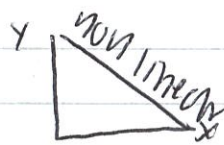
a residual is a value's distance away from the least squares regression line  $\star y - y_p$  diff b/w observed and predicted

an outlier is a data point that ~~is~~ has a high residual from the least squares regression line

what is a residual plot?



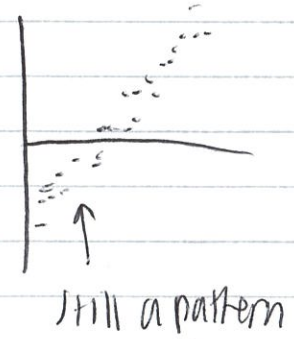
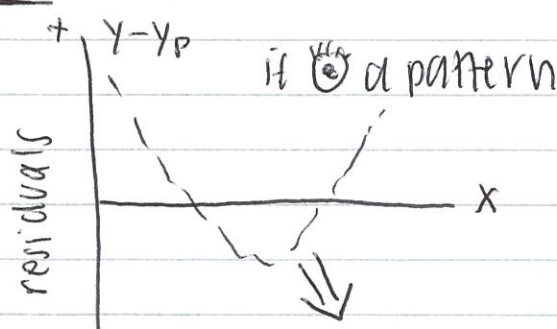
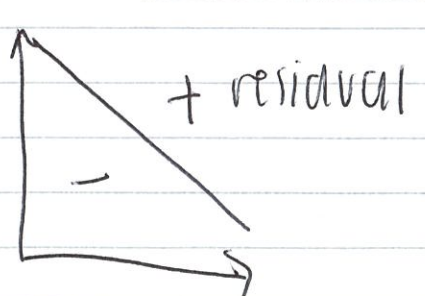
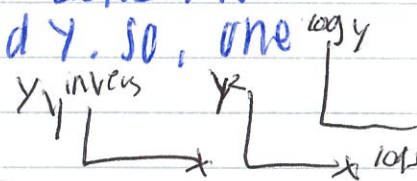
if you see a pattern



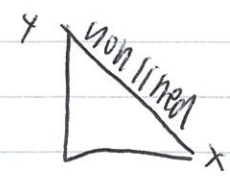
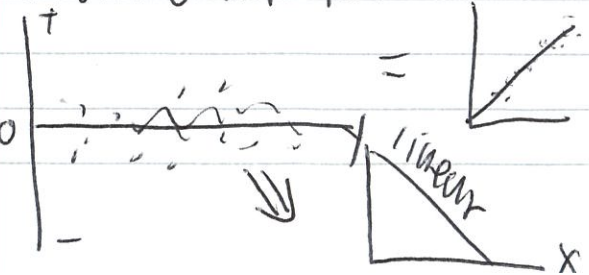
An influential observation is a data point / value that has a relatively small residual but the x is far off from majority of the data ~~is~~ exact answers in GC residual packet

why is (24, 76000) influential (ex: 4.10) the x value is far from the other values even though the point is close to the LSRL. 4 years is a lot

if the residual plot shows a pattern, then the LSRL is NOT good representation of the relationship for x and y. so, one type of transformation could be done with



if don't see a pattern



## COLLEGE BOARD VIDEO NOTES 2.7 RESIDUALS 11/10/2023

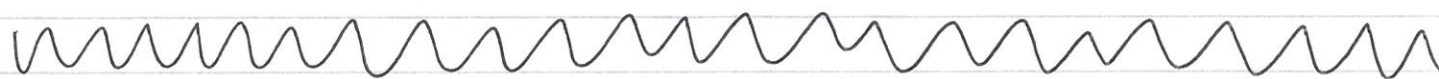
**RESIDUAL PLOT** -  $(y - \hat{y}_p)$  plot showing the residuals and fit of the least squares regression line

### GOOD FIT

- apparent randomness
- center at 0
- no clear patterns

### BAD FIT

- curve pattern
- not best fit line
- accentuate possible trends



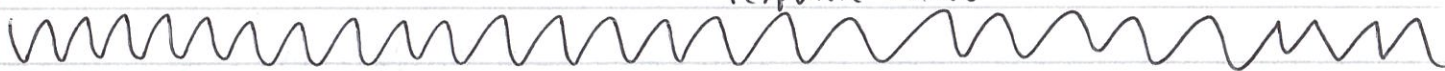
## 2.7B RESIDUALS

**residual** - the difference b/w the actual response value and the model's predicted response value

$$\text{observed } y - \text{predicted } \hat{y}$$
$$y - \hat{y}$$

**+**: model underestimated actual response value

**-**: model overestimated actual response value



## 2.9A ANALYZING DEPARTURES FROM LINEARITY

$\bar{x}$  and  $\bar{y}$  will be on the LSRL

### Low Leverage points

- LSRL shifts down

### High Leverage points

- LSRL shifts up/steeper
- points with large/small  $x$  values (far from  $\bar{x}$ )
- affect slope/ $y$ -int

### outlier

- unusually high magnitude residual
- big effect on strength of relationship

### influential points

- outliers (correlation)
- high-leverage (slope/ $y$ -int)