

CMS



6.1 Random Variables 12/04/2023

X

-QUANTITATIVE

Discrete Random Variables

-quantitative, but countable (integers) ~ whole / negative / 0

Continuous Random Variables

-quantitative, but infinite / not countable ~ fractions / decimals

pg 198 EXAMPLE 1

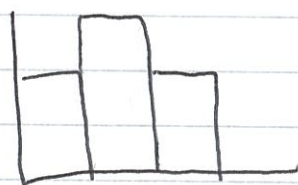
Measure the time it takes a student selected at random to register for the fall term - continuous

Count the number of bad checks drawn on Upright Bank on a day selected at random - discrete

probability distribution

-add to +1 because

no gaps and no overlaps



↙ Xs

↙ disjointed

center and spread



expected value / #

$$\mu = \sum x \cdot p(x)$$



standard deviation

$$\sigma^2 = \text{var}(x) = \sum (x - \mu)^2 \cdot p(x)$$

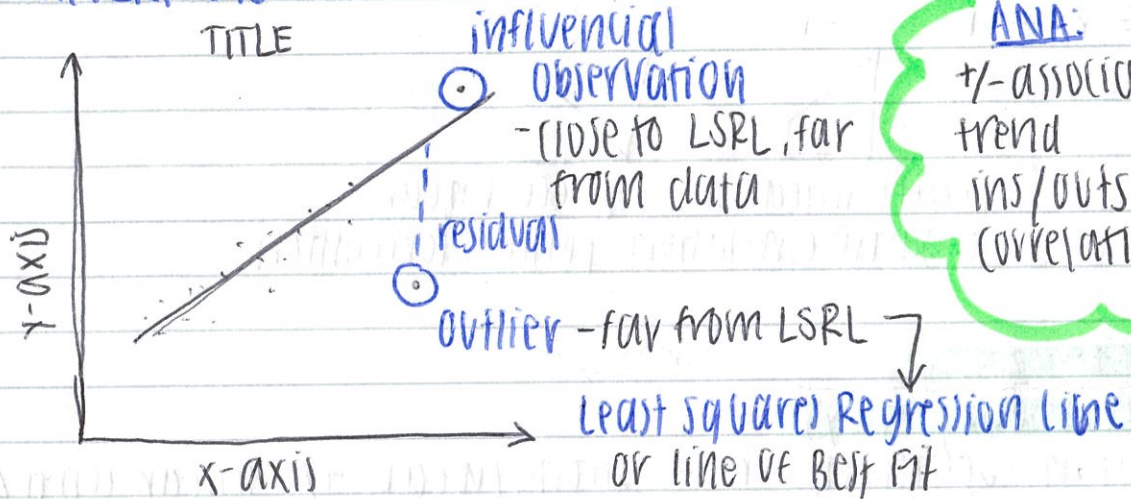
$$\sigma = \text{SD}(x) = \sqrt{\sum (x - \mu)^2 \cdot p(x)}$$

UNIT 4:

(CHAPTER 9)

BIVARIATE DATA: scatterplots, correlation coefficient, residual plot

SCATTERPLOTS:



→ finding the LSRL

1. find b → $b = \frac{n\sum xy - \sum x \sum y}{n\sum x^2 - (\sum x)^2} = \text{slope}$
2. find a → $a = \bar{y} - b\bar{x} = y - jnt$
3. plug into line equation → $\hat{y} = a + bx$
4. plot 2 points
 - b and \bar{x}, \bar{y}
 - if no b , pick a random #

→ example: $\Sigma = \text{sum of } \bar{x} = \text{mean}$

$$\begin{aligned} \bar{x} &= 3.25 & b &= \frac{n\sum xy - \sum x \sum y}{n\sum x^2 - (\sum x)^2} \\ \bar{y} &= 38.5 & &= \frac{4(411) - (13)(154)}{4(65) - (13)^2} \\ \sum x &= 13 & &= \frac{164 - 169}{-3} \\ \sum y &= 154 & &= -3.93 \text{ (1)} \\ \sum xy &= 411 & & \\ \sum x^2 &= 65 & & \end{aligned}$$

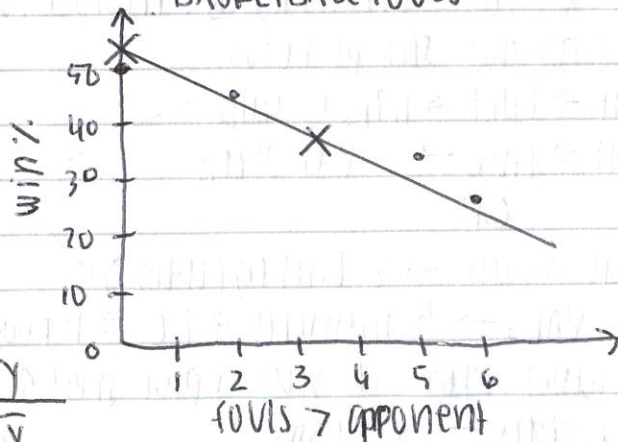
$$a = \bar{y} - b\bar{x} = 38.5 - (-3.93)(3.25)$$

$$a = 51.27 \text{ (2)}$$

$$\hat{y} = 51.27 + (-3.93)x \text{ (3)}$$

x	y
\bar{x}	\bar{y}
3.25	38.5
0	51.27

BASKETBALL FOULS



UNIT 5:

(CHAPTER 4)

PROBABILITY: compound events, p/c, tree diagram / z-table

probability - likelihood of an event happening $0 \leq P \leq 1$

$$\frac{f}{n} = \frac{\# \text{ of desired}}{\# \text{ of total}}$$

impossible

certainty

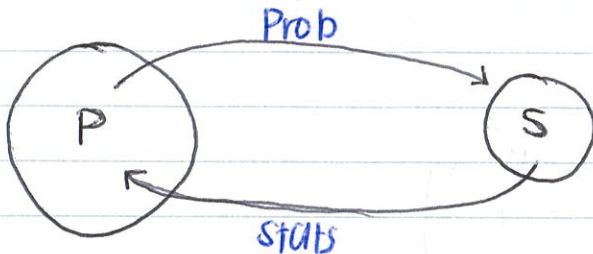
(complement - P (not the event))

$$\therefore P(A') = 1 - P(A)$$

odds - ratio

$$FAV : UNFAV$$

$$FAV : FAV'$$



conditional probability = $\frac{P(A \text{ and } B)}{P(B)}$

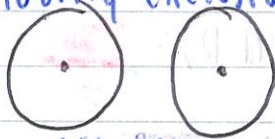
LOL #s - law of large #s

- must use large samples in case of a lucky streak ruins data / makes it more probable than it actually is

sample space = S { set of all possible outcomes }

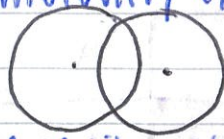
COMPOUND EVENTS:

mutually exclusive



disjoint

nonmutually exclusive



non-disjoint

$\exists X \in S$

no gaps / overlaps in sample space

COMPOUND EVENTS

$P(A \text{ and } B)$

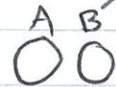
IND

$$P(A) \cdot P(B)$$

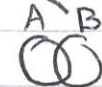
DEP

$$P(A) \cdot P(B|A)$$

$P(A \text{ OR } B)$



$$P(A) + P(B)$$



$$P(A) + P(B) - P(A \text{ and } B)$$

replace vs. no replace

6.2 BINOMIAL EXPERIMENTS 12/08/23

pg 212 STUDY GUIDE:

1. Who was Jacob Bernoulli?

17th century Swiss mathematician

2. The set of problems which have exactly 2 possible outcomes is called

$S = \{Y, N\}$ binomials

3. Describe the central problem of a binomial experiment

probability $\frac{r(\text{successes})}{n(\text{trials})}$

4. T/F Binomial experiments work only w/ dependent situations

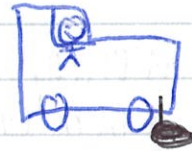
5. Each faculty member @ Pepperdine has been asked abt recommending which new car Mr. Milek should purchase: 500 members

of trials, $n = 500$

of possible outcomes =
Binomial Experiment?

NO. More than 2
Outcomes

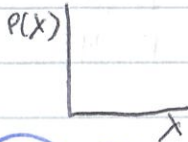
Amount of cars



Discrete random variable Bv

μ = expected value

σ



Bi

Continuous
Discrete
-2, -1, 0, 1, 2...

Success/Fail
Independent

n (predetermined # of trials)

P = goal
published research
central probability $\frac{r}{n}$

$$\mu = \sum x \cdot p(x)$$

$$\sigma = \sqrt{\sum (x - \mu)^2 \cdot p(x)}$$

TABLE WAY

HYBRID TOMATO Table 3 $n=6$

$$n=6 \quad p=0.7 \quad q=0.3 \quad r=4$$

$$0.324 = P(r=4)$$

$$P(r \geq 4) = 0.324 + 0.303 + 0.118 \\ = 0.745$$

CALL WAY

$P(r=8)$ POP QUIZ a, b, l, d, e

$$n=10 \quad r=8 \quad p=0.2 \quad q=0.8$$

$$P(r=8) = 7.37 \times 10^{-5} \\ \approx 0$$

2nd \rightarrow vars

A: binompdf(

EDPUZZLE NOTES: THE BINOMIAL DISTRIBUTION (C 12/15)



Binomial Distribution Formula:

$$\text{binom}(n, k) = {}^n C_k (p)^k (1-p)^{n-k} \text{ video's}$$

$$C_{n,r} (p)^r (1-p)^{n-r} \text{ ours / textbooks}$$

Binomial Coefficient Formula - how many ways
a certain ratio of successes to failures can occur

$${}^n C_k \text{ aka } {}^n C_r$$

n choose k

Factorials!

$$\frac{n!}{(n-k)! k!}$$





$$\text{expected \#} = n \times p$$

Bernoulli Distribution

$$P(X=1) p^1 (1-p)^{1-1} = p \text{ succ (p)}$$

$$P(X=0) p^0 (1-p)^{1-0} = (1-p) \text{ fail}$$

5.2 #18 one-time thing! (with clushes)

trial =  

incl? yes

S = "yes"

F = "no"

$$P(r) = C_{n,r} p^r q^{n-r}$$

$p = 0.1$

$n = 7$

$q = 0.9$

$r = 2$

$$P(r=2) = C_{7,2} (0.1)^2 (0.9)^{7-2}$$

$$= 21 (0.01) (0.5905)$$

$$P(r \leq 2) = P(0) + P(1) + P(2)$$

$$= 0.4783 + 0.3720 + 0.1240$$

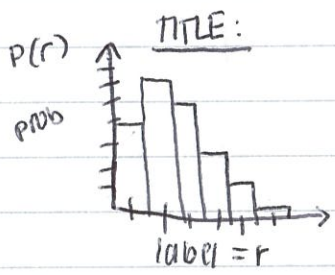
$$P(r=2) = \underline{\underline{0.1240}}$$

$$P(r \leq 2) = \underline{\underline{0.9743}}$$

TABLE WAY:

$$P(2 \leq r \leq 6) = 0.124 + 0.023 + 0.003 + 0.000 + 0.000$$

$$= \underline{\underline{0.15}}$$



ANA ^{ean}
 $M = 1.5$
 Shp: skewed high
 Spr: $\sigma = 1.0607$
 o: 4+ "mod. high"

$n = 6$
 $P = 0.25$

$r = 0$	$= 0.178$
1	$= 0.356$
2	$= 0.309$
3	$= 0.132$
4	$= 0.033$
5	$= 0.007$
6	$= 0.000$

} table

5.1
 $\mu = \sum x \cdot p(x)$

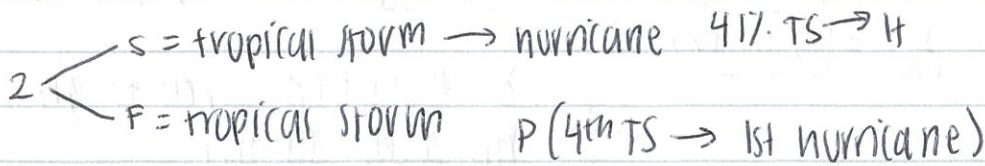
- ▶ $\mu = np = 6(0.25)$
- ▶ $\sigma = \sqrt{npq} = \sqrt{1.125}$

- ▶ AA (an appreciation)
- ▶ MUESNER 40 years $p = 0.8$ P/F incl 20 sts



CB GEOMETRIC DISTRIBUTIONS VID 12/14/23

HURRICANE EX



hurricane = 74+ mph
independent

$p = 0.41$

$q = 0.59$

\rightarrow binomial would be $1/4$ instead of $1/4$

$H = \#$ tropical storms to get first hurricane

GEOMETRIC:

- 2 outcomes (F/S)
- independent trials
- each trial has same prob of S

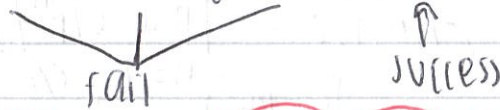
BINOMIAL:

- fixed # of trials

$P(H=4) = (1-0.41)(1-0.41)(1-0.41)(0.41) = 0.0842$



probability notation



$P(X=x) = (1-p)^{x-1} p$ for $x = 1, 2, 3, \dots$

$q^{n-1} p$

Cumulative Geometric Prob:

$P(H \leq 3)$

$P(X=4) = \text{geompdf}(p=0.53, x=4) = 0.055$

mean: $\mu_x = \frac{1}{p}$

SD: $\sigma_x = \frac{\sqrt{1-p}}{p} \rightarrow q$

8.26 n PACKET

$S =$ defective disk drive 1st messed up on the 5th
 $F =$ working / not ddd
 Independent $X =$ # of disks until the first ddd is the
 $p = 0.03$ $n = ??$ 5th unit tested
 $q = 0.97$ stop @ 1st success

x	1	2	3	4	5
$P(x)$	0.03	$F \cdot S$ $q \cdot p$ $0.97 \cdot 0.03$ 0.0291	$q \cdot q \cdot p$ 0.0282	0.0274	0.0266
			$q^{n-1} p$		

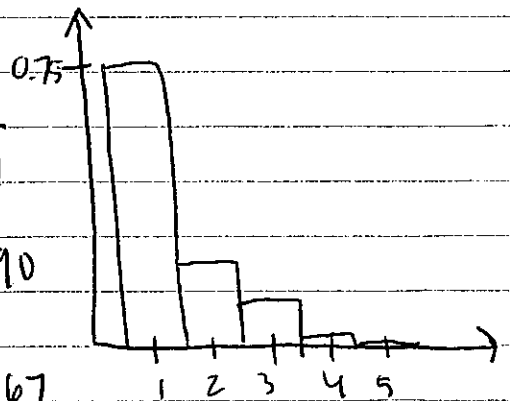
8.41 (COIN TOS)

$S \left\{ \begin{array}{l} 1 \quad 2 \quad 3 \\ h \quad h \quad h \\ h \quad h \quad t \\ h \quad t \quad h \\ t \quad h \quad h \\ t \quad t \quad h \\ t \quad h \quad t \\ h \quad t \quad t \\ t \quad t \quad t \end{array} \right\}$ "wins"
 \rightarrow 1 odd man

a.) 0.25 ~~75~~
 $p =$
 $6/8 = 0.75$
 $q = 0.25$

d.)

x	1	2	3	4	5
$P(x)$	0.75	0.1875	0.0469	0.0117	0.0029
CUMV	0.75	0.9375	0.9844	0.9961	0.9990



$\mu = \frac{1}{0.75} = 1.33$ $\sigma = \frac{\sqrt{1-p}}{p} = 0.67$

CHAPTER 9 (Unit 6) REVIEW PROBS 12/18/23

pg 242 #26 EXTROVERTED PROFESSOR

BINOMIAL

trial = testing a professor's personality

S = extroverted

F = introverted

$p = 0.45$

$n = 6$

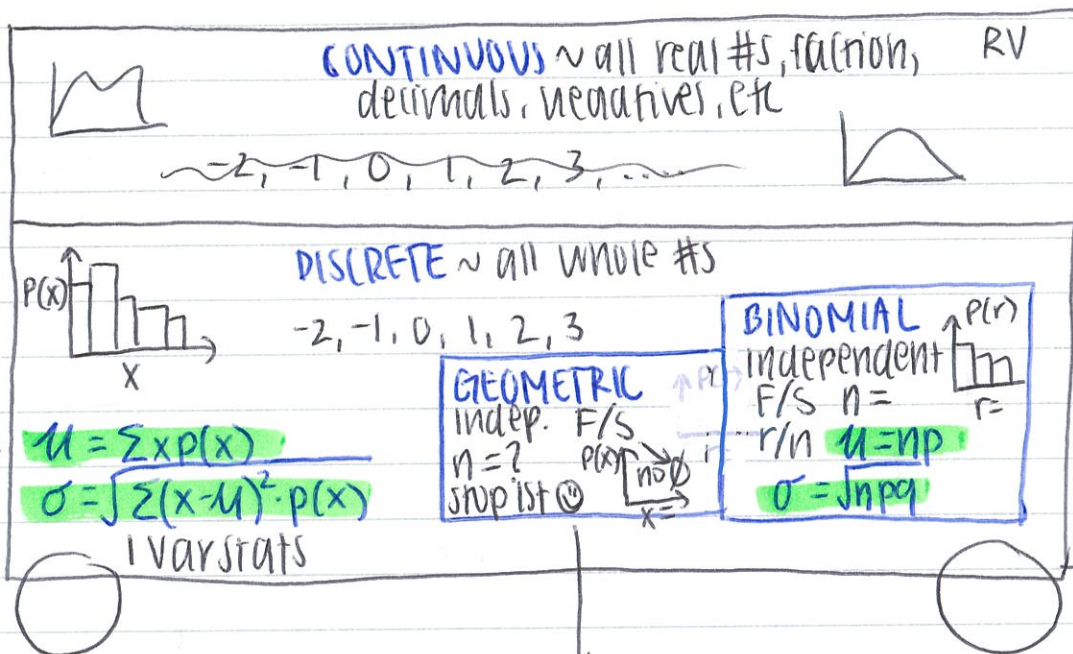
$r = 6$

$P(r=6) = 0.0083$.83% highly unlikely

UNIT 6 =

(CHAPTER 5)

Random variations, Probability distributions, Binomials, Geometric



expected value $\mu = \sum x p(x)$

$p = \text{success}$
 $q = \text{fail}$

can't succeed on
oth trial!

$\mu = \frac{1}{p}$
 $\sigma = \frac{\sqrt{q}}{p}$

$P(X > n) = (1-p)^n$

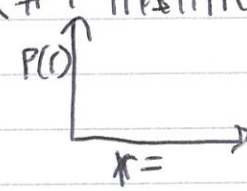
ANA:
C: $\mu =$
S:
S: $\sigma \sim \text{word}$
O: $< 5\%$

→ BINOMIAL

EQUATION METHOD: $C_{n,r} p^r q^{n-r}$ ★ # + likelihood

TABLE METHOD: $n = ?$ $p = ?$ add em up

CALCULATOR METHOD: 2nd → vars
A: binompdf



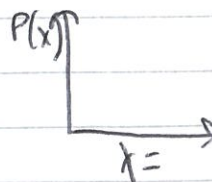
→ GEOMETRIC ~ stop until success ★ Prob. Notation + # + likelihood

$p q^{n-1}$

define x

Ex: $x = \#$ of litters born to get 1st large family

x	1	2	3	4
$p(x)$	p	$q \cdot p$	$q \cdot q \cdot p$	$q \cdot q \cdot q \cdot p$

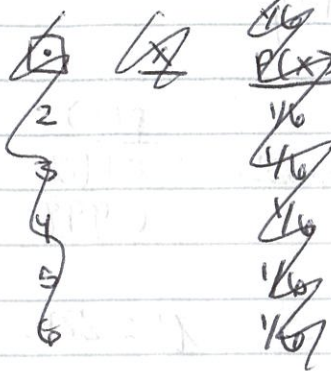


OR: 2nd → var
F: geometpdf

DISCRETE VALUE REVIEW 1/10/24

(C)	x	P(x)	x · P(x)
H	\$2	0.5	1 · 0.5
T	\$2	0.5	0 · 0.5

$$\mu = \sum xP(x)$$



x	P(x)
1	1/6
2	1/6
3	1/6
4	1/6
5	1/6
6	1/6

DISCRETE VALUE REVIEW

informal

$$\mu = 2.54$$

$$\sigma = 1.3669$$

1	2	3	4	5
27%	31%	18%	9%	15%



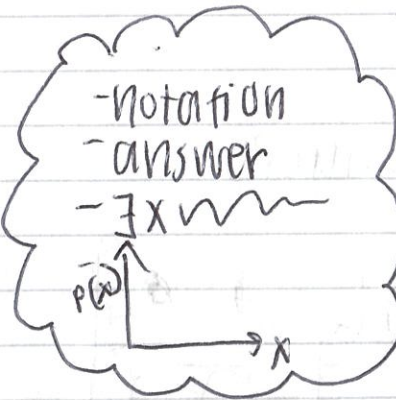
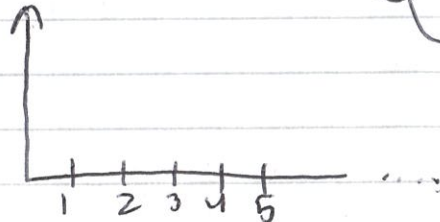
Bad Business

$$P(X \leq 3) = P(1) + P(2) + P(3)$$

$$= 0.02 + 0.07 + 0.15$$

$$= 0.24$$

Ex a 24% that a business will fail within 3 years



xP(x)
8/6
-2/6
-2/6
-2/6
-2/6
-2/6
$\mu = \sum = -2/6 = \$-13$

$$P(X > 6) = 0.21 \quad \text{Ex 21\% chance that a business ends after 6 years}$$

$$\mu = 4.98 \text{ years}$$

